

GATE ECE 2027 MASTER HANDBOOK

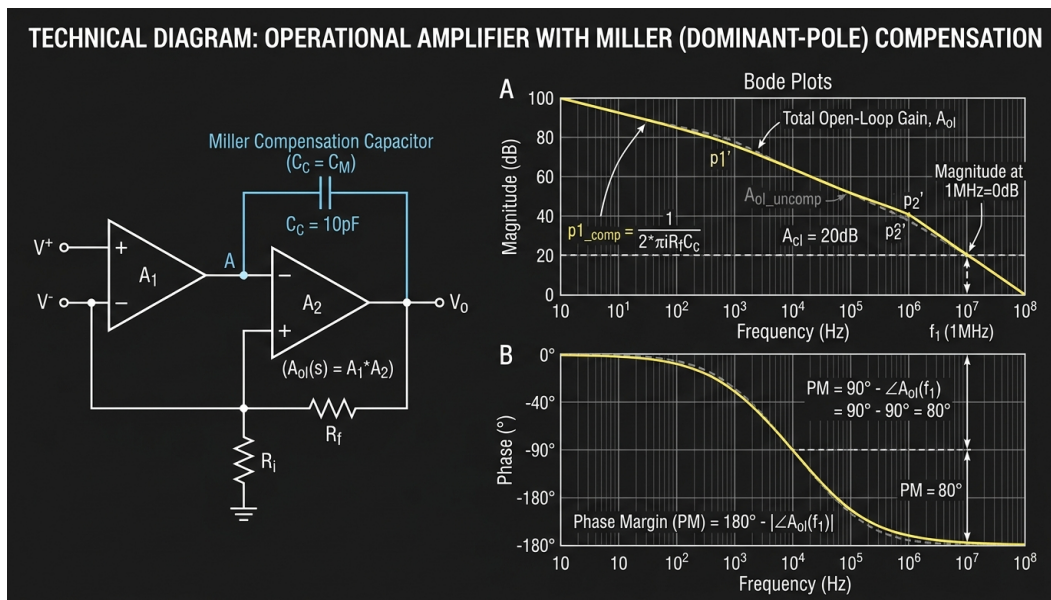
Complete Strategy, Concept Notes, Revision Formulae & Question Bank
Organizing Institute: IIT Madras (Official GATE 2027 Syllabus)

1. Executive Strategy & GATE 2027 Syllabus Analysis

This master handbook provides an exhaustive guide for candidates preparing for **GATE ECE 2027 organized by IIT Madras**. It combines high-yield concept derivations, shortcut formulas, visual circuit schematics, and solved previous-year questions.

Key Syllabus Additions for GATE 2027 (IIT Madras):

- **Signals & Systems:** FIR & IIR Filter Design (Window methods, Bilinear transformation, frequency pre-warping) and Signal Reconstruction.
- **Engineering Mathematics:** Correlation & Regression Analysis (Pearson's r , linear regression slopes b_{yx} , b_{xy}) and Euler-Cauchy ODEs.
- **Analog Circuits:** Dominant-pole Miller Compensation & Phase Margin stability criteria.
- **Control Systems:** PID Controllers (P, I, D action impact on rise time, overshoot, steady-state error) and Compensators.
- **Communications:** Source Coding Theorem (Shannon source coding, Huffman coding, efficiency) under Information Theory.



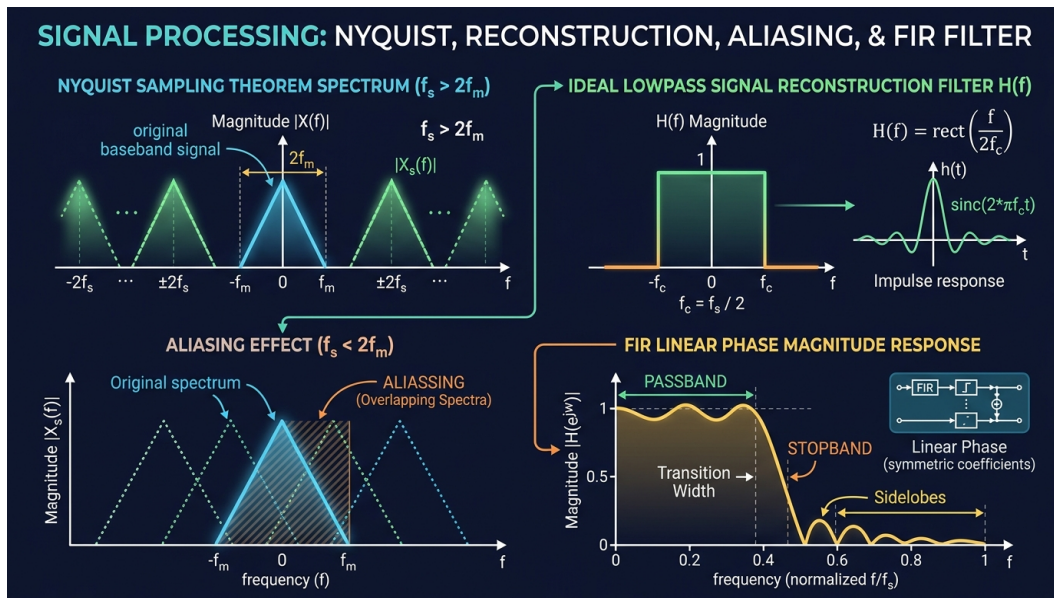
2. Section-Wise Concept Building Notes

Engineering Mathematics (~13 Marks)

- **Linear Algebra:** $\text{Trace}(A) = \text{Sum of diagonal} = \text{Sum of eigenvalues}$; $\text{Det}(A) = \text{Product of eigenvalues}$.
- **Euler-Cauchy ODE:** $x^2 y'' + a x y' + b y = f(x) \rightarrow \text{Substitute } x = e^z \rightarrow D(D-1)y + aDy + by = f(e^z)$.
- **Correlation & Regression:** $r = \frac{\text{Cov}(X,Y)}{(\sigma_X \cdot \sigma_Y)} = \sqrt{b_{yx} \cdot b_{xy}}$. Regression: $Y - \bar{Y} = b_{yx}(X - \bar{X})$.

Signals & Systems (~12 Marks)

- **Sampling & Reconstruction:** $f_s \geq 2 f_m$. Reconstruction filter sinc interpolation: $x(t) = \sum x(n T_s) \text{sinc}((t - n T_s)/T_s)$.
- **Bilinear Transform:** $s = (2/T_s) * (1 - z^{-1})/(1 + z^{-1})$. Pre-warping: $\Omega = (2/T_s) \tan(\omega/2)$.



Network Theory (~12 Marks)

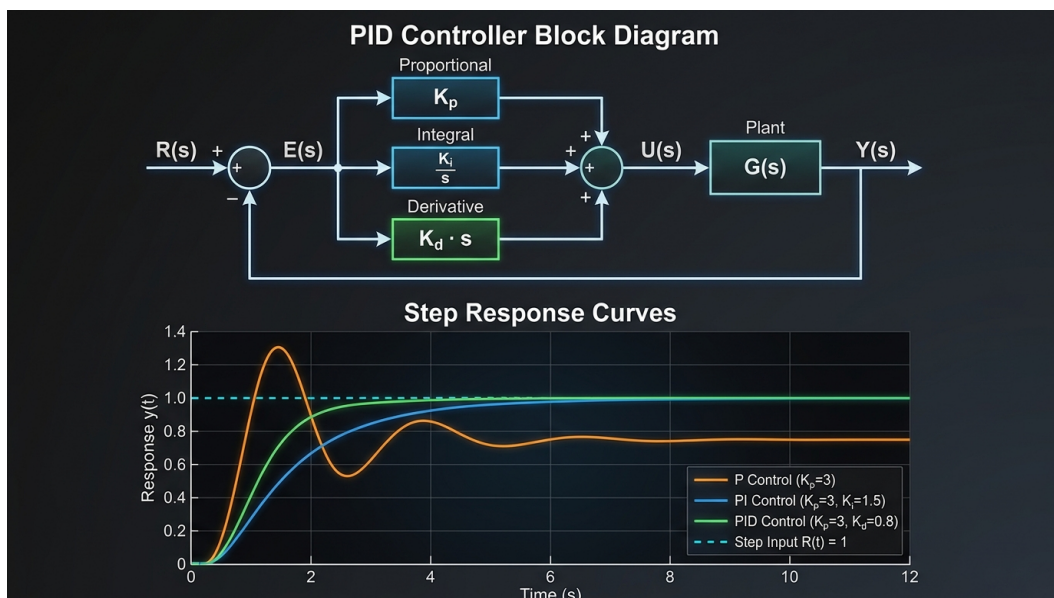
- **Transient Response:** $x(t) = x(\infty) + [x(0+) - x(\infty)] e^{-(t/\tau)}$. $\tau = RC$ or L/R .
- **Max Power Transfer:** Complex load $Z_L = Z_{th}^*$ $\rightarrow P_{max} = |V_{th}|^2 / (4 R_{th})$. Resistive load $R_L = |Z_{th}|$.

Analog Circuits (~10 Marks)

- **Miller Compensation:** Pole splitting causes dominant pole $p_1' = 1/(2\pi R_{in} A_2 C_C)$. $GBW = g_{m1} / (2\pi C_C)$.
- **Phase Margin:** $PM = 180^\circ + \angle(T(j\omega_{gc}))$. Target $PM \geq 60^\circ$ for optimal stability.

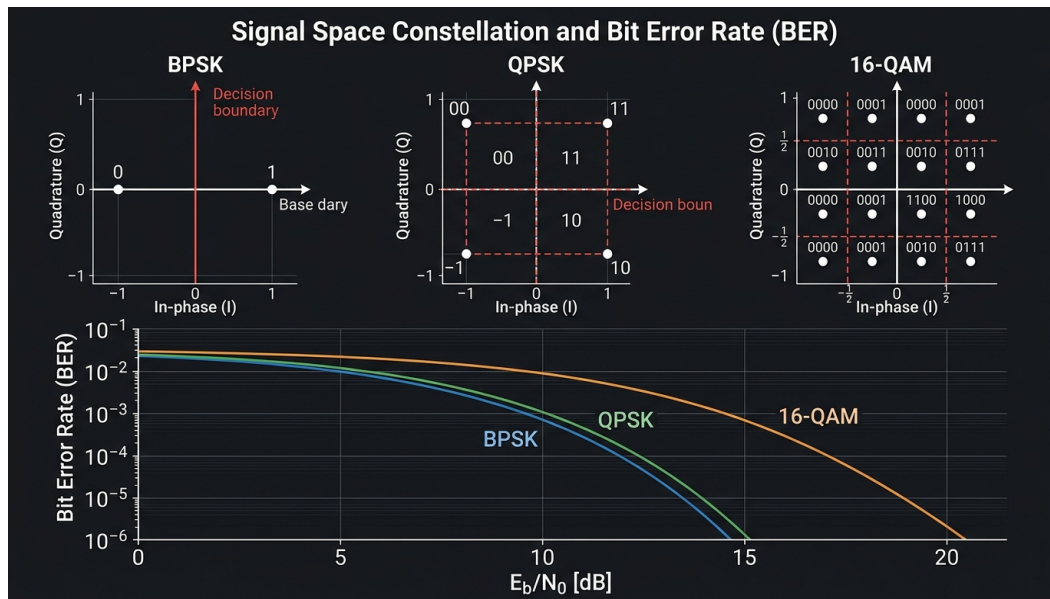
Control Systems (~9 Marks)

- **PID Controller:** $G_c(s) = K_p + K_i/s + K_d s$. Integral action eliminates e_{ss} ($e_{ss} \rightarrow 0$). Derivative action improves stability & reduces overshoot M_p .



Communication Systems (~13 Marks)

- **Information Theory:** $H(X) = \sum P_i \log_2(1/P_i)$. Source Efficiency $\eta = H(X) / L_{\text{bar}}$.
- **Digital Modulation:** BPSK $P_e = Q(\sqrt{2 E_b / N_0})$, QPSK $P_e = Q(\sqrt{2 E_b / N_0})$.



3. Selected GATE Solved Numerical Examples

Example 1: Linear Regression Coefficient (Engineering Maths)

Problem: Given regression slopes $b_{yx} = 0.8$ and $b_{xy} = 0.45$, find correlation coefficient r .

Solution: $r = \sqrt{b_{yx} \cdot b_{xy}} = \sqrt{0.8 \cdot 0.45} = \sqrt{0.36} = \mathbf{0.60}$.

Example 2: Op-Amp Miller Bandwidth (Analog Circuits)

Problem: First stage $g_{m1} = 1$ mA/V, Miller capacitor $C_C = 10$ pF. Find GBW in MHz.

Solution: $GBW = g_{m1} / (2\pi C_C) = 10^{-3} / (2\pi \cdot 10^{-11}) = 10^8 / (2\pi) = \mathbf{15.92 \text{ MHz}}$.

Example 3: PD Controller Parameters (Control Systems)

Problem: Plant $G(s) = 1/s^2$ controlled by $G_c(s) = K_p + K_d s$. Target poles $s = -2 \pm j2$.

Solution: Characteristic Eq: $s^2 + K_d s + K_p = (s+2)^2 + 4 = s^2 + 4s + 8 = 0 \rightarrow \mathbf{K_d = 4, K_p = 8}$.